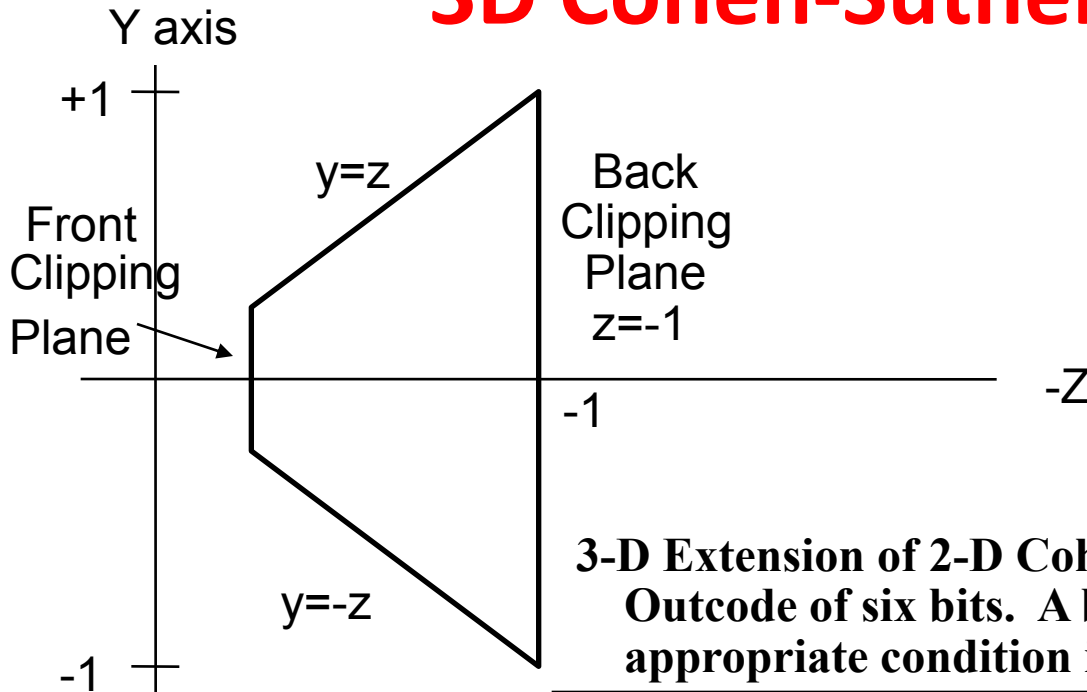


3D Clipping & Viewing process

3D Cohen-Sutherland Algorithm



3-D Extension of 2-D Cohen-Sutherland Algorithm, Outcode of six bits. A bit is true (1) when the appropriate condition is satisfied

Bit 1 - Point is above view volume	$y > -z$
Bit 2 - Point is below view volume	$y < z$
Bit 3 - Point is right of view volume	$x > -z$
Bit 4 - Point is left of view volume	$x < z$
Bit 5 - Point is behind view volume	$z < -1$
Bit 6 - Point is in front of view volume	$z > z_{min}$

3D Cohen-Sutherland Algorithm

- A line is trivially accepted if both endpoints have a code of all zeros.
- A line is trivially rejected if the bit-by-bit logical AND of the codes is not all zeros.
- Otherwise Calculate intersections.

On the $y = z$ plane from parametric equation of the line:

$$y_0 + t(y_1 - y_0) = z_0 + t(z_1 - z_0)$$

Solve for t and calculate x and y . Already know $z = y$

3D Cohen-Sutherland Algorithm

- If t not between $[0, 1]$, then the intersection is not between P_0 and P_1
 - $t = (z_0 - y_0) / [(y_1 - y_0) - (z_1 - z_0)]$
- If t between $[0, 1]$, then use t to find x and y
 - $x = x_0 + [(x_1 - x_0)(z_0 - y_0)] / [(y_1 - y_0) - (z_1 - z_0)]$
 - $y = y_0 + [(y_1 - y_0)(z_0 - y_0)] / [(y_1 - y_0) - (z_1 - z_0)]$

3D viewing process

- Specify a 3D view volume
 - $\mathbf{N}_{per} = [\mathbf{S}_{per}][\mathbf{SH}_{per}][\mathbf{T}(-\mathbf{PRP})][\mathbf{R}][\mathbf{T}(-\mathbf{VRP})]$
- Clip against view volume
- Project onto a 2D viewing plane
 - $\mathbf{M}_{per} : d = -\mathbf{PRP}_n$
- Apply 2D viewing transformations to map window contents into 2D-image viewport
 - $\mathbf{V} = [\mathbf{T}^{-1}][\mathbf{S}][\mathbf{T}]$

3D viewing Transformation 3D to 2D

3D to 2D

$$P'(x',y',z',w) = [\mathbf{M}_{\text{per}}][\mathbf{N}_{\text{per}}][P(x,y,z,1)]$$

2D to Image

$$P''(x,y,1) = [\mathbf{V}][P(x'/w,y'/w,1)]$$