## Digital Signatures \& Authentication Protocols

## Digital Signatures

- have looked at message authentication
- but does not address issues of lack of trust
- digital signatures provide the ability to:
- verify author, date \& time of signature
- authenticate message contents
- be verified by third parties to resolve disputes


## Digital Signature Properties

- must depend on the message signed
- must use information unique to sender
- to prevent both forgery and denial
- must be relatively easy to produce
- must be relatively easy to recognize \& verify
- be computationally infeasible to forge
- with new message for existing digital signature
- with fraudulent digital signature for given message
- be practical save digital signature in storage


## Direct Digital Signatures

- involve only sender \& receiver
- assumed receiver has sender's public-key
- digital signature made by sender signing entire message or hash with private-key
- can encrypt using receivers public-key
- important that sign first then encrypt message \& signature
- security depends on sender's private-key


## Arbitrated Digital Signatures

- involves use of arbiter $A$
- validates any signed message
- then dated and sent to recipient
- requires suitable level of trust in arbiter
- can be implemented with either private or public-key algorithms
- arbiter may or may not be able to see message


## Authentication Protocols

- used to convince parties of each others identity and to exchange session keys
- may be one-way or mutual
- key issues are
- confidentiality - to protect session keys
- timeliness - to prevent replay attacks
- published protocols are often found to have flaws and need to be modified


## Replay Attacks

- where a valid signed message is copied and later resent
- simple replay
- repetition that can be logged
- repetition that cannot be detected
- backward replay without modification
- countermeasures include
- use of sequence numbers (generally impractical)
- timestamps (needs synchronized clocks)
- challenge/response (using unique nonce)


## Using Symmetric Encryption

- as discussed previously, we can use a two-level hierarchy of keys
- usually with a trusted Key Distribution Center (KDC)
- each party shares own master key with KDC
- KDC generates session keys used for connections between parties
- master keys used to distribute these to them


## Needham-Schroeder Protocol

- original third-party key distribution protocol
- for session between A B mediated by KDC
- protocol overview is:

1. A->KDC: $I D_{A}\left\|I D_{B}\right\| N_{1}$
2. $\mathrm{KDC}->\mathrm{A}: \mathrm{E}_{\text {Ka }}\left[K s\left\|I D_{B}\right\| N_{1} \| \mathrm{E}_{K b}\left[K s \| \mid I D_{A}\right]\right]$
3. A $\rightarrow \mathrm{B}: E_{K b}\left[K s| | I D_{A}\right]$
4. B $->$ A: $E_{K s}\left[N_{2}\right]$
5. A $\rightarrow \mathrm{B}: E_{K S}\left[f\left(N_{2}\right)\right]$

## Needham-Schroeder Protocol

- used to securely distribute a new session key for communications between A \& B
- but is vulnerable to a replay attack if an old session key has been compromised
- then message 3 can be resent convincing $B$ that is communicating with A
- modifications to address this require:
- timestamps (Denning 81)
- using an extra nonce (Neuman 93)


## Using Public-Key Encryption

- have a range of approaches based on the use of public-key encryption
- need to ensure have correct public keys for other parties
- using a central Authentication Server (AS)
- various protocols exist using timestamps or nonces


## Denning AS Protocol

- Denning 81 presented the following:

$$
\text { 1. A -> AS: } I D_{A} \| I D_{B}
$$

$$
\text { 2. AS -> A: } \mathrm{E}_{\mathrm{PRas}}\left[I D_{A}\left\|\mathrm{P} U_{a}\right\| \mathrm{T}\right] \| \mathrm{E}_{\mathrm{PRas}}\left[I D_{B}\left\|\mathrm{PU}_{b}\right\| \mathrm{T}\right]
$$

$$
\text { 3. A -> B: } \mathrm{E}_{\mathrm{PRas}\left[I D_{A}\left\|\mathrm{P} U_{a}\right\| \mathrm{T}\right]\left\|\mathrm{E}_{\mathrm{PRas}}\left[I D_{B}\left\|\mathrm{PU}_{b}\right\| \mathrm{T}\right]\right\| . . \mid}
$$ $\mathrm{E}_{\mathrm{PUb}}\left[\mathrm{E}_{\mathrm{PRas}}\left[\mathrm{K}_{s} \| \mathrm{T}\right]\right]$

- note session key is chosen by $A$, hence AS need not be trusted to protect it
- timestamps prevent replay but require synchronized clocks


## One-Way Authentication

- required when sender \& receiver are not in communications at same time (e.g., email)
- have header in clear so can be delivered by email system
- may want contents of body protected \& sender authenticated


## Using Symmetric Encryption

- can refine use of KDC but can't have final exchange of nonces:

1. A->KDC: $I D_{A}\left\|I D_{B}\right\| N_{1}$
2. $\mathrm{KDC}->\mathrm{A}: \mathrm{E}_{\mathrm{Ka}}\left[K s\left\|I D_{B}\right\| N_{1} \| \mathrm{E}_{K b}\left[K s \| I D_{A}\right]\right]$
3. $\mathrm{A}->\mathrm{B}: E_{K b}\left[K s| | I D_{A}\right]| | E_{K s}[M]$

- does not protect against replays
- could rely on timestamp in message, though email delays make this problematic


## Public-Key Approaches

- have seen some public-key approaches
- if confidentiality is major concern, can use:

A->B: $\mathrm{E}_{\text {Pus }}[\mathrm{Ks}] \| \mathrm{E}_{\mathrm{Ks}}[\mathrm{M}]$

- has encrypted session key, encrypted message
- if authentication needed, use a digital signature with a digital certificate:
A->B: $M\left|\mid E_{P R a}[H(M)] \| E_{P R a s}\left[T| | I D_{A} \| P U_{a}\right]\right.$
- with message, signature, certificate


## Digital Signature Standard (DSS)

- US Govt approved signature scheme
- designed by NIST \& NSA in early 90's
- published as FIPS-186 in 1991
- revised in 1993, 1996 \& then 2000
- uses the SHA hash algorithm
- DSS is the standard, DSA is the algorithm
- FIPS 186-2 (2000) includes alternative RSA \& elliptic curve signature variants


## Digital Signature Algorithm (DSA)

- creates a 320 bit signature
- with 512-1024 bit security
- smaller and faster than RSA
- a digital signature scheme only
- security depends on difficulty of computing discrete logarithms
- variant of ElGamal \& Schnorr schemes


## Digital Signature Algorithm (DSA)


(a) RSA Approach

(b) DSS Approach

## DSA Key Generation

- have shared global public key values ( $\mathrm{p}, \mathrm{q}, \mathrm{g}$ ):
- choose q, a 160 bit
- choose a large prime $p=2^{\mathrm{L}}$
- where L= 512 to 1024 bits and is a multiple of 64
- and q is a prime factor of $(\mathrm{p}-1)$
- choose $g=h(p-1) / q$
- where $h<p-1, h^{(p-1) / q}(\bmod p)>1$
- users choose private \& compute public key:
- choose $\mathrm{x}<\mathrm{q}$
- compute $y=g^{x}(\bmod p)$


## DSA Signature Creation

- to sign a message M the sender:
- generates a random signature key $k$, $k<q$
- $k$ must be random, be destroyed after use, and never be reused
- then compute signature pair:

$$
\begin{aligned}
& r=\left(g^{k}(\bmod p)\right)(\bmod q) \\
& s=\left(k^{-1} \cdot H(M)+x \cdot r\right)(\bmod q)
\end{aligned}
$$

- sends signature ( $r, s$ ) with message $M$


## DSA Signature Verification

- having received M \& signature ( r , s )
- to verify a signature, recipient computes:

$$
\begin{aligned}
& \mathrm{w}=\mathrm{s}^{-1}(\bmod \mathrm{q}) \\
& \mathrm{u} 1=(\mathrm{H}(\mathrm{M}) \cdot \mathrm{w})(\bmod \mathrm{q}) \\
& \mathrm{u} 2=(\mathrm{r} \cdot \mathrm{w})(\bmod q) \\
& \mathrm{v}=\left(\mathrm{g}^{\mathrm{u} 1} \cdot \mathrm{y}^{\mathrm{u} 2}(\bmod \mathrm{p})\right)(\bmod q)
\end{aligned}
$$

- if $\mathrm{v}=r$ then signature is verified
- see book web site for details of proof why


## Summary

- have discussed:
- digital signatures
- authentication protocols (mutual \& one-way)
- digital signature algorithm and standard

