satellite navigation and the global positioning systems.

Satellite Tracking

To "track" a satellite, one needs to be able to point one's antenna at it. This requires calculating the azimuth and elevation angles satellite. for the Fundamentally, this is a geometry problem, which is discussed in section 2.5.2 of the text.



Satellite Navigation

Navigation means calculating the location of the spot being sensed. This is also a complex geometry problem which is discussed in section 2.5.3 of the text.



Space-Time Sampling

How often is a particular point observed? This topic is covered in section 2.6 of the text.



MetSat Orbits

- Geostationary
- Sunsynchronous
- LEO
- MEO
- Molniya
- Formations
- Constellations

Geostationary Orbit

Geostationary satellites remain at a constant radius, latitude (0°), and longitude. Let's construct the orbital elements:

- 1. Circular orbit $\rightarrow \varepsilon = 0$
- 2. Stays at equator $\rightarrow i = 0$
- 3. Orbits at the same speed that the earth rotates (7.292115922 x 10^{-5} radians/s) $\rightarrow a = 42,168$ km
- 4. Ω doesn't matter for $i \approx 0$
- 5. ω doesn't matter for $\varepsilon \approx 0$
- 6. Choose *M* (consistent with Ω and ω) so that the satellite is at the desired longitude.

 $\phi = \sin^{-1}(\sin\Gamma \sin i)$ highest latitude = i

~ 6.6 earth radii

Geostationary Orbit



Geostationary Ground Track



Sunsynchronous Orbits

The right ascension of ascending node changes:

$$\frac{d\Omega}{dt} = -\overline{n} \left[\frac{3}{2} J_2 \left(\frac{r_{ee}}{a} \right)^2 \left(1 - \varepsilon^2 \right)^{-2} \cos i \right]$$

The inclination angle can be chosen such that Ω changes at the same rate that the earth orbits the sun, 2π radians per tropical year or 0.98565°/day.

Note that $i > 90^{\circ}$ (retrograde) for a sunsynchronous orbit. For NOAA satellites, $i \approx 99^{\circ}$.

Equator Crossing Time



Sunsynchronous Orbital Elements

- 1. Choose *a* for the period that you want
- 2. Circular orbit $\rightarrow \varepsilon = 0$
- 3. Calculate *i* from $d\Omega/dt$ formula to make a sunsynchronous orbit
- 4. ω doesn't matter for a circular orbit
- 5. Choose Ω for the equator crossing time that you want (and launch at the right time)
- 6. *M* doesn't really matter because the orbits shift daily.

Sunsynchronous Groundtrack

NOAA II Three Orbits on 22 March 1990 Start time: 0258 UTC End time: 0804 UTC Polar regions are observed every orbit



Equatorial regions are observed twice per day per satellite

a = 7229.606 km i = 98.97446° € = 0.00119958 Mo=192.28166°

 $\omega_0 = 167.74754^\circ$

 $\Omega_0 = 29.3059^\circ$

- Epoch time = 22 Mar 1990 1^h 15^m 52.353^s UTC
- Nodal Period = 102.0764 min

Formations

For two satellites to fly in formation, their orbital elements must be related.

- Their semimajor axes must be identical--else they would have different periods and would separate)
- Their inclination angles must be identical--else they would veer left and right)
- Their eccentricities must be identical (preferably zero) else they would oscillate up and down



EO-1 flies 1 min behind Landsat 7 SAC-C flies 27 min behind EO-1 Terra flies 2.5 min behind SAC-C

• And...

Formations...

• Their mean anomalies and arguments of perigee must be related.

Let Δt be the desired separation time. Then their angular separation must be:

$$\Delta\Gamma = \Delta (M + \omega) = 360^{\circ} \frac{\Delta t}{\tilde{T}}$$

Assumes a circular orbit, for which $M = \theta$

• Their right ascensions of ascending node must be related so that they travel over the same ground track:

$$\Delta \Omega = \frac{d\Omega_{earth}}{dt} \Delta t$$

Launch Vehicles

Boeing's Delta II



Payload delivery options range from about 1-2 metric tons (1,980 to 4,550 lb) to geosynchronous transfer orbit (GTO) and 2.7 to 5.8 metric tons (6,020 to 12,820 lb) to low-Earth orbit (LEO).