NETWORK ANALYSIS AND SYNTHESIS

Unit – III
Transient Circuit Analysis

- Natural response and forced response,

- Transient response and steady state response for arbitrary inputs (DC and AC),

- Evaluation of time response both through classical and Laplace methods.

Solution to First Order Differential Equation

Consider the general Equation

$$\tau \frac{dx(t)}{dt} + x(t) = K_s f(t)$$

Let the initial condition be $x(t = 0) = x(0)$, then we solve the differential equation:

$$\tau \frac{dx(t)}{dt} + x(t) = K_s f(t)$$

The complete solution consists of two parts:
• the homogeneous solution (natural solution)
• the particular solution (forced solution)

The Natural Response

Consider the general Equation

$$\tau \frac{dx(t)}{dt} + x(t) = K_S f(t)$$

Setting the excitation $f(t)$ equal to zero,

$$\tau \frac{dx_N(t)}{dt} + x_N(t) = 0 \ or \quad \frac{dx_N(t)}{dt} = -\frac{x_N(t)}{\tau}, \frac{dx_N(t)}{x_N(t)} = -\frac{dt}{\tau}$$

$$\int \frac{dx_N(t)}{x_N(t)} = \int -\frac{dt}{\tau}, \qquad x_N(t) = \alpha\, e^{-t/\tau}$$

It is called the natural response.

The Forced Response

Consider the general Equation

$$\tau \frac{dx(t)}{dt} + x(t) = K_S f(t)$$

Setting the excitation $f(t)$ equal to F, a constant for $t \geq 0$

$$\tau \frac{dx_F(t)}{dt} + x_F(t) = K_S F$$

$$x_F(t) = K_S F \ \ for \ t \geq 0$$

It is called the forced response.

The Complete Response

Consider the general Equation

$$\tau \frac{dx(t)}{dt} + x(t) = K_S f(t)$$

The complete response is:
- **the natural response** +
- **the forced response**

$$x = x_N(t) + x_F(t)$$

$$= \alpha e^{-t/\tau} + K_S F$$

$$= \alpha e^{-t/\tau} + x(\infty)$$

Solve for α,

$$for \ t = 0$$

$$x(t = 0) = x(0) = \alpha + x(\infty)$$
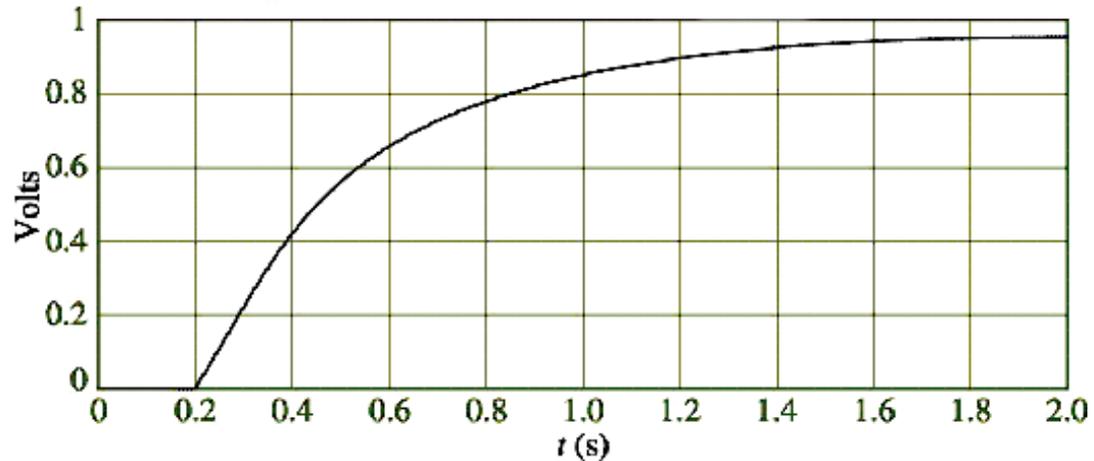
$$\alpha = x(0) - x(\infty)$$

The Complete solution:

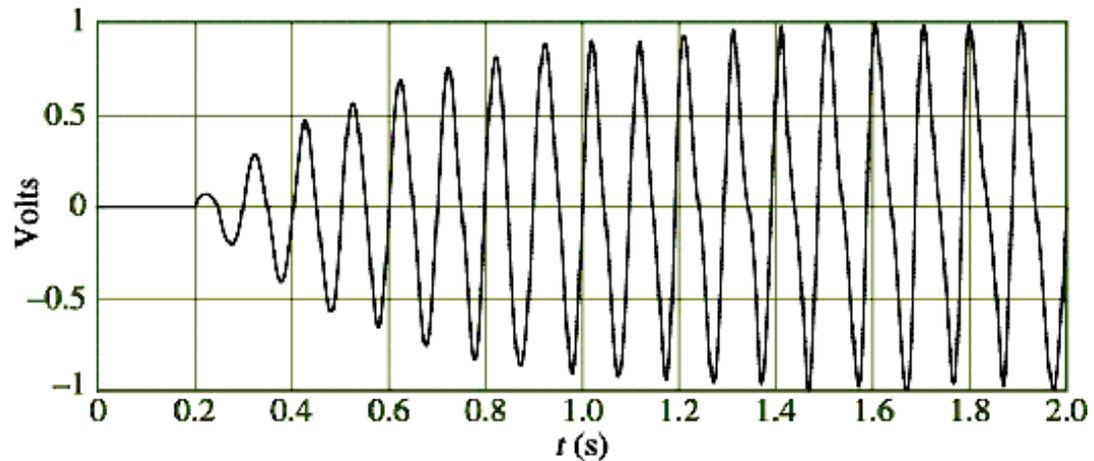$$x(t) = [x(0) - x(\infty)] e^{-t/\tau} + x(\infty)$$

$[x(0) - x(\infty)] e^{-t/\tau}$ **called transient response**

$x(\infty)$ **called steady state response**

WHAT IS TRANSIENT RESPONSE

(a) Transient DC voltage

(b) Transient sinusoidal voltage

THANKS….

Queries Please…