## NETWORK ANALYSIS AND SYNTHESIS

## Two Port Networks

## Y parameters:

$$
\begin{aligned}
& y_{11}=\left.\frac{I_{1}}{V_{1}}\right|_{V_{2}=0} \\
& y_{12}=\left.\frac{I_{1}}{V_{2}}\right|_{V_{1}=0}
\end{aligned}
$$

$\mathrm{y}_{11}$ is the admittance seen looking into port 1 when port 2 is shorted.
$\mathrm{y}_{12}$ is a transfer admittance. It is the ratio of the current at port 1 to the voltage at port 2 when port 1 is shorted.
$y_{21}=\left.\frac{I_{2}}{V_{1}}\right|_{V_{2}=0}$
$\mathrm{y}_{21}$ is a transfer impedance. It is the ratio of the current at port 2 to the voltage at port 1 when port 2 is shorted.

$$
y_{22}=\left.\frac{I_{2}}{V_{2}}\right|_{V_{1}=0}
$$

$\mathrm{y}_{22}$ is the admittance seen looking into port 2 when port 1 is shorted.

## Two Port Networks

## Z parameters: <br> Example 1

Given the following circuit. Determine the $Z$ parameters.


Find the Z parameters for the above network.

## Two Port Networks

## Z parameters:

Example 1 (cont 1)

## For $\mathrm{z}_{11}$ :

$$
Z_{11}=8+20| | 30=20 \Omega
$$

## For $\mathrm{z}_{12}$ :

$$
\left.z_{12}=\frac{V_{1}}{I_{2}} \right\rvert\, I_{1}=0
$$

$$
V_{1}=\frac{20 x I_{2} x 20}{20+30}=8 x I_{2}
$$

$$
\text { For } z_{22} \text { : }
$$

$$
Z_{22}=20| | 30=12 \Omega
$$



Therefore:

$$
z_{12}=\frac{8 x I_{2}}{I_{2}}=8 \Omega=z_{21}
$$

## Two Port Networks

## Z parameters: <br> Example 1 (cont 2)

The $Z$ parameter equations can be expressed in matrix form as follows.

$$
\begin{aligned}
& {\left[\begin{array}{l}
V_{1} \\
V_{2}
\end{array}\right]=\left[\begin{array}{ll}
z_{11} & z_{12} \\
z_{21} & z_{22}
\end{array}\right]\left[\begin{array}{l}
I_{1} \\
I_{2}
\end{array}\right]} \\
& {\left[\begin{array}{c}
V_{1} \\
V_{2}
\end{array}\right]=\left[\begin{array}{cc}
20 & 8 \\
8 & 12
\end{array}\right]\left[\begin{array}{l}
I_{1} \\
I_{2}
\end{array}\right]}
\end{aligned}
$$

## Two Port Networks

## Z parameters:

Example 2 (problem 18.7 Alexander \& Sadiku)

You are given the following circuit. Find the $Z$ parameters.


## THANKS....

Queries Please...

