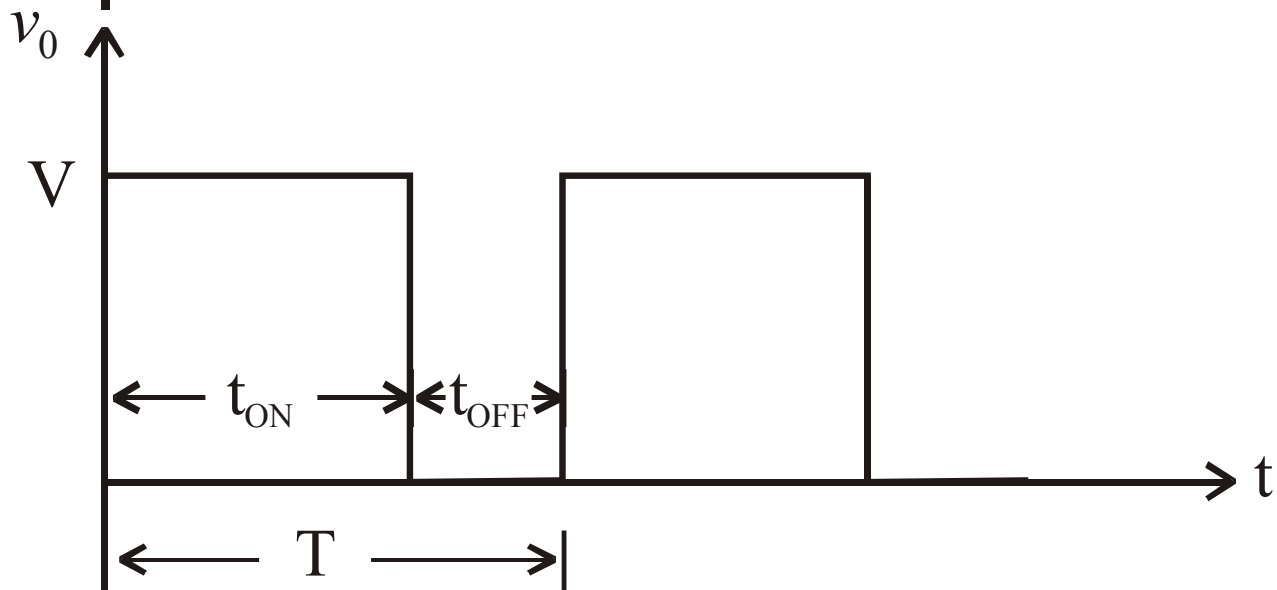
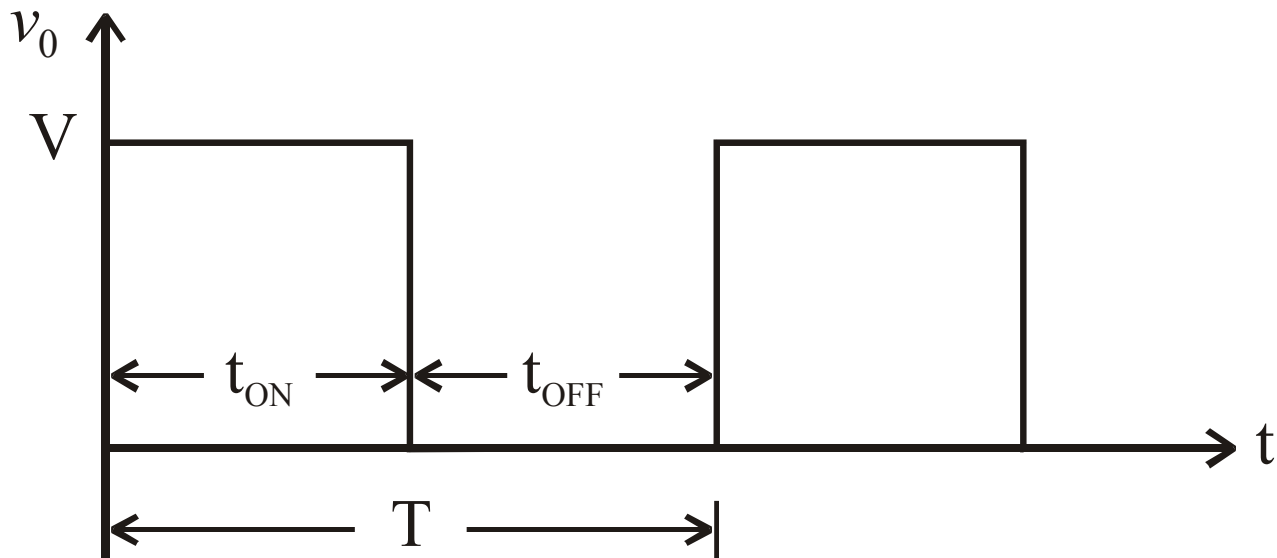


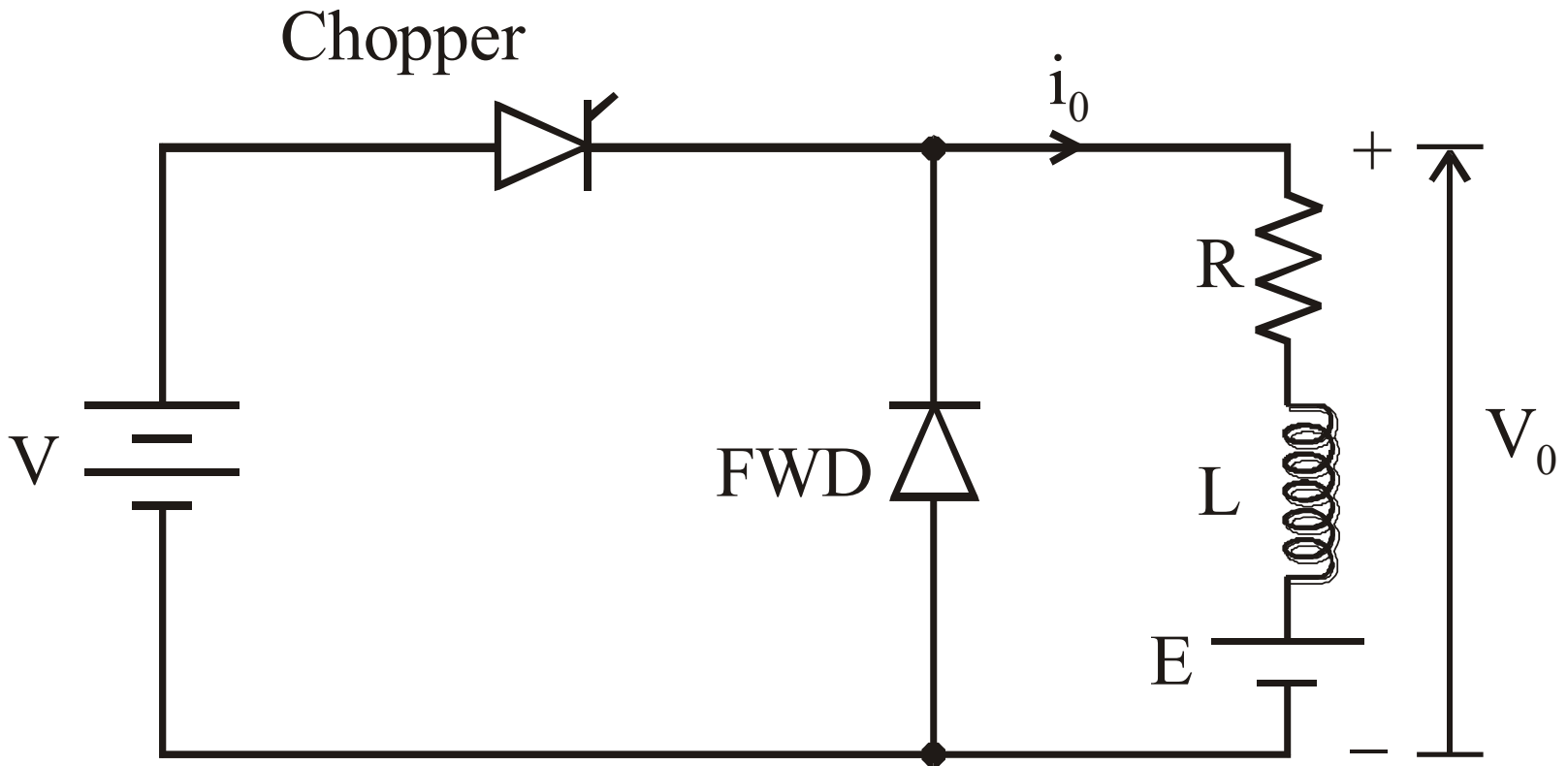
Variable Frequency Control

- Chopping frequency ' f ' is varied keeping either t_{ON} or t_{OFF} constant.
- To obtain full output voltage range, frequency has to be varied over a wide range.
- This method produces harmonics in the output and for large t_{OFF} load current may become discontinuous





Step-down Chopper With R-L Load

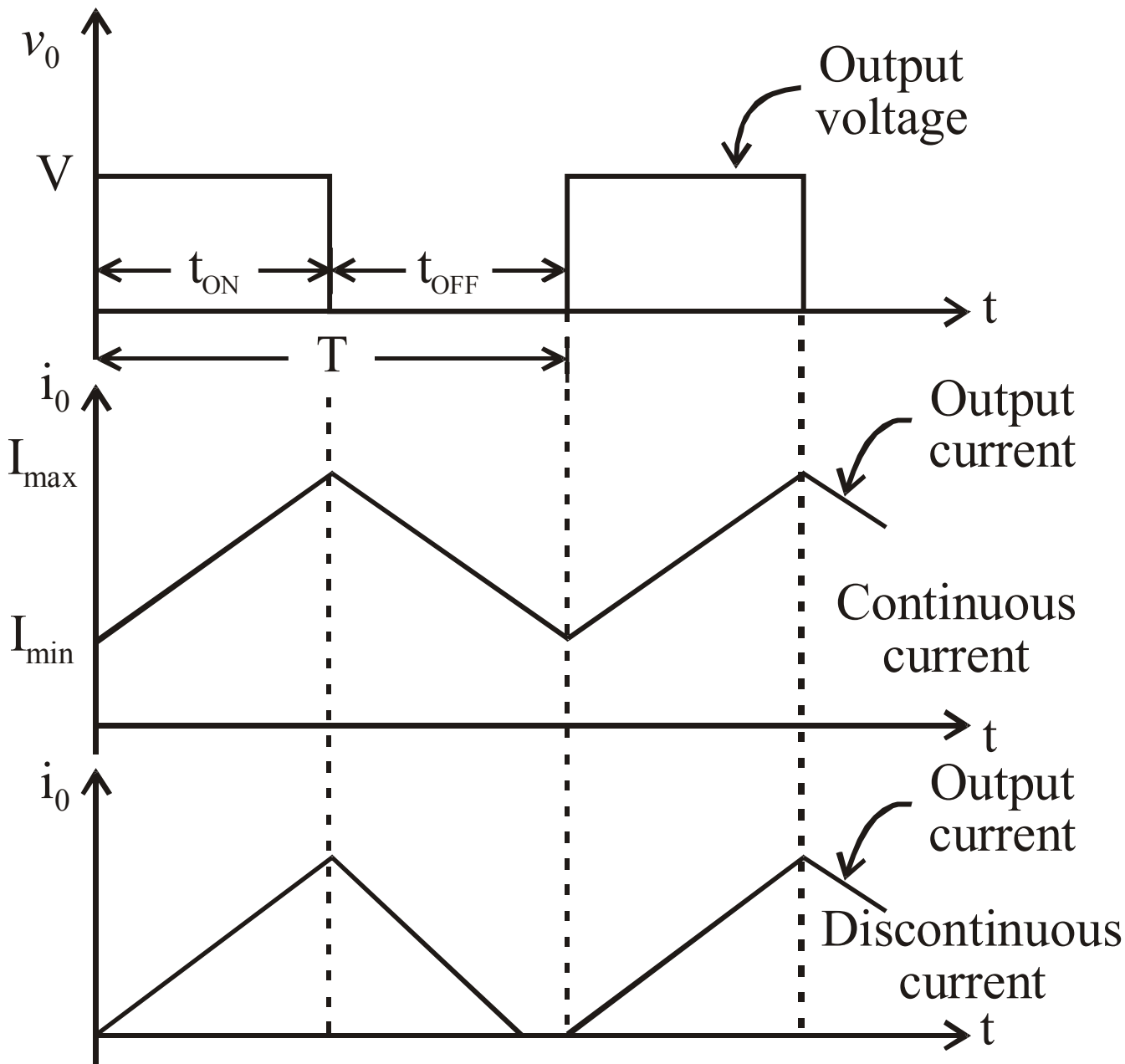


- When chopper is ON, supply is connected across load.
- Current flows from supply to load.
- When chopper is OFF, load current continues to flow in the same direction through FWD due to energy stored in inductor ' L '.



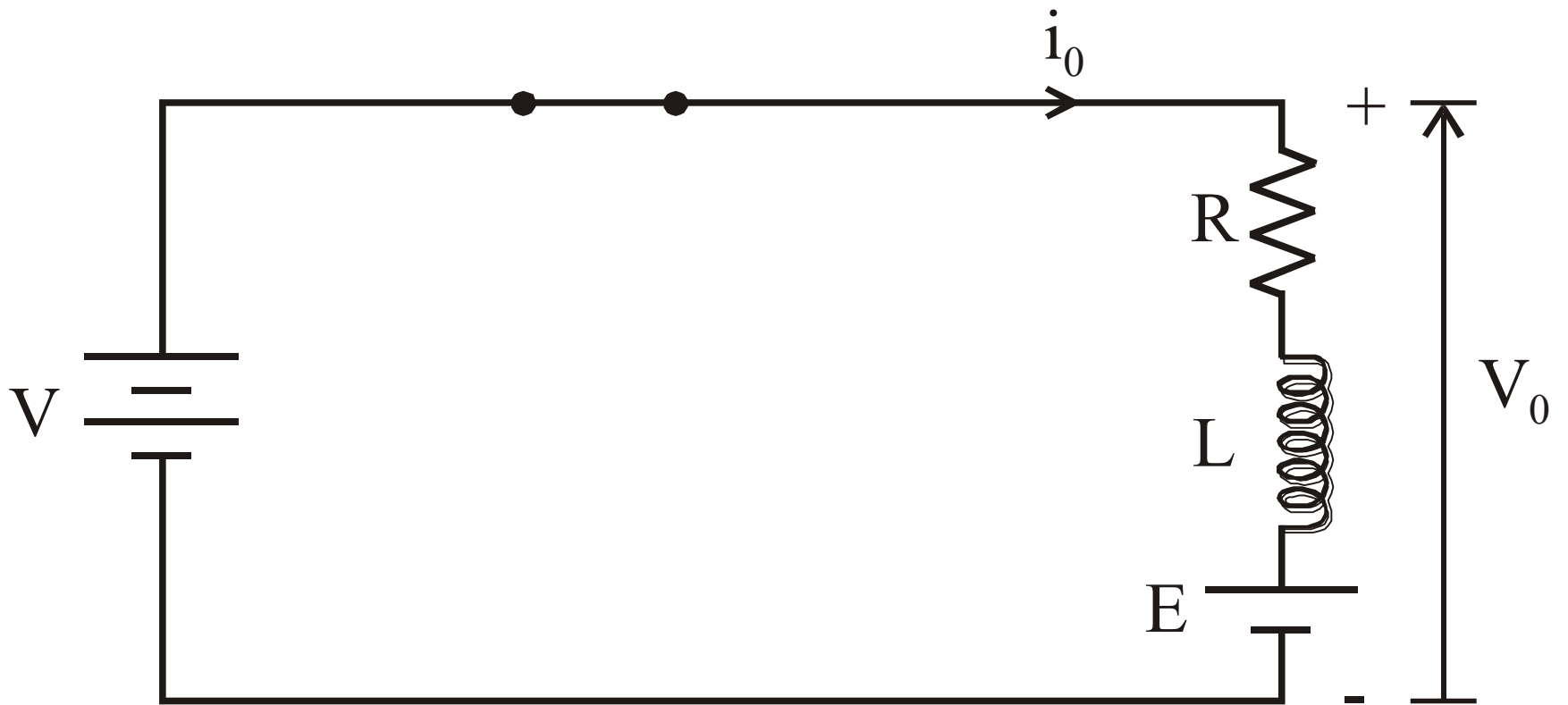
- Load current can be continuous or discontinuous depending on the values of ' L ' and duty cycle ' d '
- For a continuous current operation, load current varies between two limits I_{max} and I_{min}
- When current becomes equal to I_{max} the chopper is turned-off and it is turned-on when current reduces to I_{min} .





Expressions For
Load Current
 i_o For Continuous Current Operation
When
Chopper Is ON ($0 \leq t \leq t_{ON}$)





$$V = i_o R + L \frac{di_o}{dt} + E$$

Taking Laplace Transform

$$\frac{V}{S} = RI_o(S) + L \left[S.I_o(S) - i_o(0^-) \right] + \frac{E}{S}$$

At $t = 0$, initial current $i_o(0^-) = I_{\min}$

$$I_o(S) = \frac{V - E}{LS \left(S + \frac{R}{L} \right)} + \frac{I_{\min}}{S + \frac{R}{L}}$$



Taking Inverse Laplace Transform

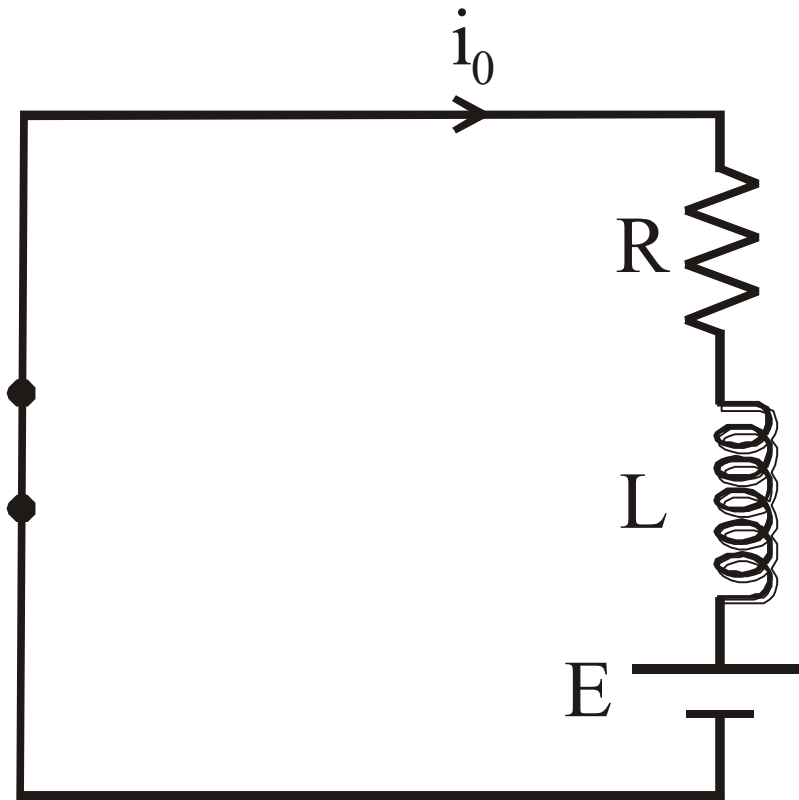
$$i_o(t) = \frac{V - E}{R} \left[1 - e^{-\left(\frac{R}{L}\right)t} \right] + I_{\min} e^{-\left(\frac{R}{L}\right)t}$$

This expression is valid for $0 \leq t \leq t_{ON}$,
i.e., during the period chopper is ON.

At the instant the chopper is turned off,
load current is $i_o(t_{ON}) = I_{\max}$



When Chopper is OFF



When Chopper is OFF ($0 \leq t \leq t_{OFF}$)

$$0 = Ri_o + L \frac{di_o}{dt} + E$$

Talking Laplace transform

$$0 = RI_o(S) + L \left[SI_o(S) - i_o(0^-) \right] + \frac{E}{S}$$

Redefining time origin we have at $t = 0$,

$$\text{initial current } i_o(0^-) = I_{\max}$$



$$\therefore I_o(S) = \frac{I_{\max}}{S + \frac{R}{L}} - \frac{E}{LS \left(S + \frac{R}{L} \right)}$$

Taking Inverse Laplace Transform

$$i_o(t) = I_{\max} e^{-\frac{R}{L}t} - \frac{E}{R} \left[1 - e^{-\frac{R}{L}t} \right]$$



The expression is valid for $0 \leq t \leq t_{OFF}$,
i.e., during the period chopper is OFF

At the instant the chopper is turned ON or at
the end of the off period, the load current is

$$i_O(t_{OFF}) = I_{\min}$$



To Find I_{\max} & I_{\min}

From equation

$$i_o(t) = \frac{V - E}{R} \left[1 - e^{-\left(\frac{R}{L}\right)t} \right] + I_{\min} e^{-\left(\frac{R}{L}\right)t}$$

At $t = t_{ON} = dT$, $i_o(t) = I_{\max}$

$$\therefore I_{\max} = \frac{V - E}{R} \left[1 - e^{-\frac{dRT}{L}} \right] + I_{\min} e^{-\frac{dRT}{L}}$$



From equation

$$i_o(t) = I_{\max} e^{-\frac{R}{L}t} - \frac{E}{R} \left[1 - e^{-\frac{R}{L}t} \right]$$

At $t = t_{OFF} = T - t_{ON}$, $i_o(t) = I_{\min}$

$$t = t_{OFF} = (1 - d)T$$



$$\therefore I_{\min} = I_{\max} e^{-\frac{(1-d)RT}{L}} - \frac{E}{R} \left[1 - e^{-\frac{(1-d)RT}{L}} \right]$$

Substituting for I_{\min} in equation

$$I_{\max} = \frac{V - E}{R} \left[1 - e^{-\frac{dRT}{L}} \right] + I_{\min} e^{-\frac{dRT}{L}}$$

we get,

$$I_{\max} = \frac{V}{R} \left[\frac{1 - e^{-\frac{dRT}{L}}}{1 - e^{-\frac{RT}{L}}} \right] - \frac{E}{R}$$



Substituting for I_{\max} in equation

$$I_{\min} = I_{\max} e^{-\frac{(1-d)RT}{L}} - \frac{E}{R} \left[1 - e^{-\frac{(1-d)RT}{L}} \right]$$

we get,

$$I_{\min} = \frac{V}{R} \left[\frac{e^{\frac{dRT}{L}} - 1}{e^{\frac{RT}{L}} - 1} \right] - \frac{E}{R}$$

$(I_{\max} - I_{\min})$ is known as the steady state ripple.



Therefore peak-to-peak ripple current

$$\Delta I = I_{\max} - I_{\min}$$

Average output voltage

$$V_{dc} = d.V$$

Average output current

$$I_{dc(\text{approx})} = \frac{I_{\max} + I_{\min}}{2}$$



Assuming load current varies linearly
from I_{\min} to I_{\max} instantaneous
load current is given by

$$i_O = I_{\min} + \frac{(\Delta I) \cdot t}{dT} \text{ for } 0 \leq t \leq t_{ON} (dT)$$

$$i_O = I_{\min} + \left(\frac{I_{\max} - I_{\min}}{dT} \right) t$$



RMS value of load current

$$I_{O(RMS)} = \sqrt{\frac{1}{dT} \int_0^{dT} i_0^2 dt}$$

$$I_{O(RMS)} = \sqrt{\frac{1}{dT} \int_0^{dT} \left[I_{\min} + \frac{(I_{\max} - I_{\min})t}{dT} \right]^2 dt}$$

$$I_{O(RMS)} = \sqrt{\frac{1}{dT} \int_0^{dT} \left[I_{\min}^2 + \left(\frac{I_{\max} - I_{\min}}{dT} \right)^2 t^2 + \frac{2I_{\min} (I_{\max} - I_{\min})t}{dT} \right] dt}$$



RMS value of output current

$$I_{O(RMS)} = \left[I_{\min}^2 + \frac{(I_{\max} - I_{\min})^2}{3} + I_{\min} (I_{\max} - I_{\min}) \right]^{\frac{1}{2}}$$

RMS chopper current

$$I_{CH} = \sqrt{\frac{1}{T} \int_0^T i_0^2 dt}$$

$$I_{CH} = \sqrt{\frac{1}{T} \int_0^T \left[I_{\min} + \left(\frac{I_{\max} - I_{\min}}{dT} \right) t \right]^2 dt}$$



$$I_{CH} = \sqrt{d} \left[I_{\min}^2 + \frac{(I_{\max} - I_{\min})^2}{3} + I_{\min} (I_{\max} - I_{\min}) \right]^{\frac{1}{2}}$$

$$I_{CH} = \sqrt{d} I_{O(RMS)}$$

Effective input resistance is

$$R_i = \frac{V}{I_S}$$



Where

$I_S = \text{Average source current}$

$$I_S = dI_{dc}$$

$$\therefore R_i = \frac{V}{dI_{dc}}$$

