

Wave- particle duality

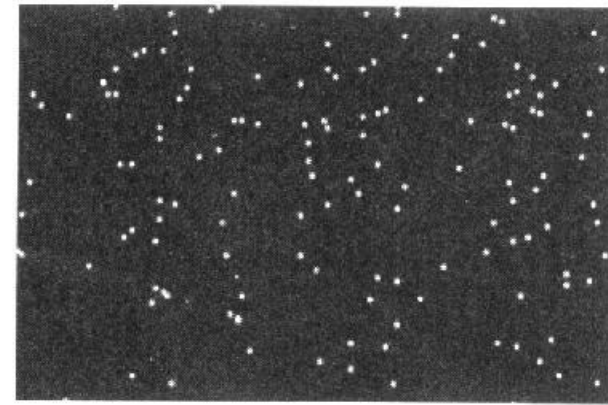
Count Louis de Broglie



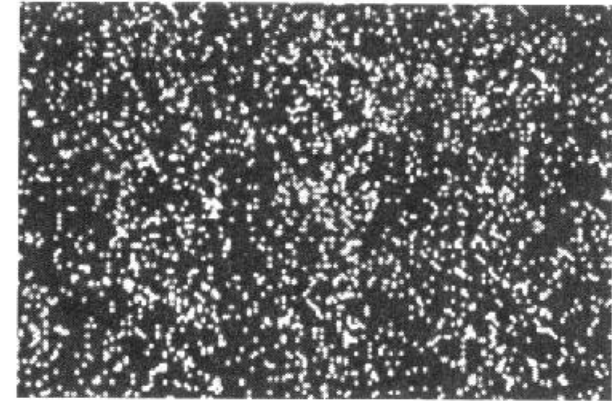
- Postulated that all objects have a wavelength given by
$$\lambda = h/p$$
 - λ =wavelength
 - h =Planck's constant
 - p =momentum of object
- In practice, only really small objects have a sensible wavelength

Wave-Particle duality

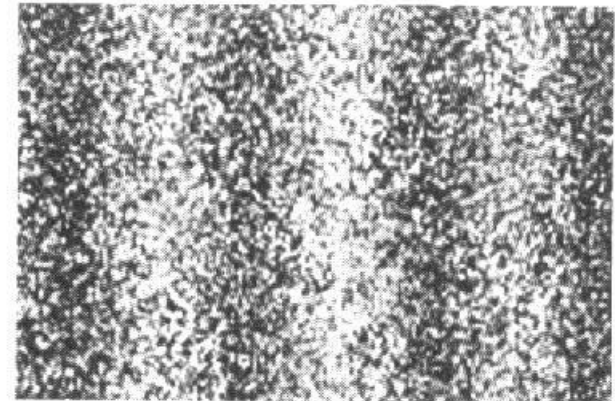
- A consequence of the deBroglie hypothesis is that all objects can be thought of as “wavicles”: both particles and waves
- This has troubled many philosophically-minded scientists over the years.
- Inescapable if we want to build atomic-resolution sensors.



(b) After 100 electrons



(c) After 3000 electrons



(d) After 70 000 electrons

Heisenberg's "Uncertainty Principle"

- Cannot simultaneously measure an object's momentum and position to a better accuracy than $\hbar/2$

$$\Delta p_x \Delta x \geq \hbar/2$$

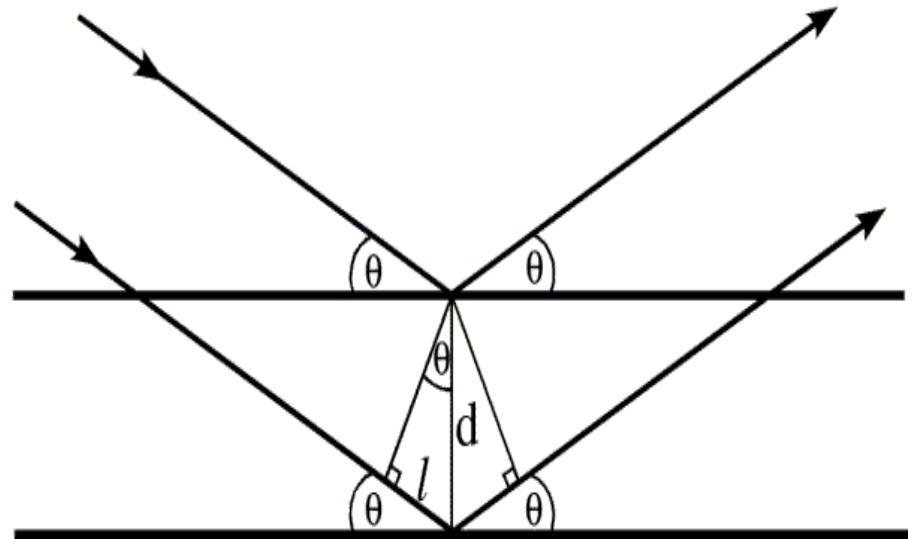
- Direct consequence of wave-particle duality
- Places limitations on sensor accuracy

Electron Diffraction

- Accelerated electrons have wavelength of order 1 Angstrom= 1×10^{-10} m
- Same order as atomic spacing
- Electrons undergo Bragg diffraction at atomic surfaces if the atoms are lined up in planes, (i.e. in a crystal)

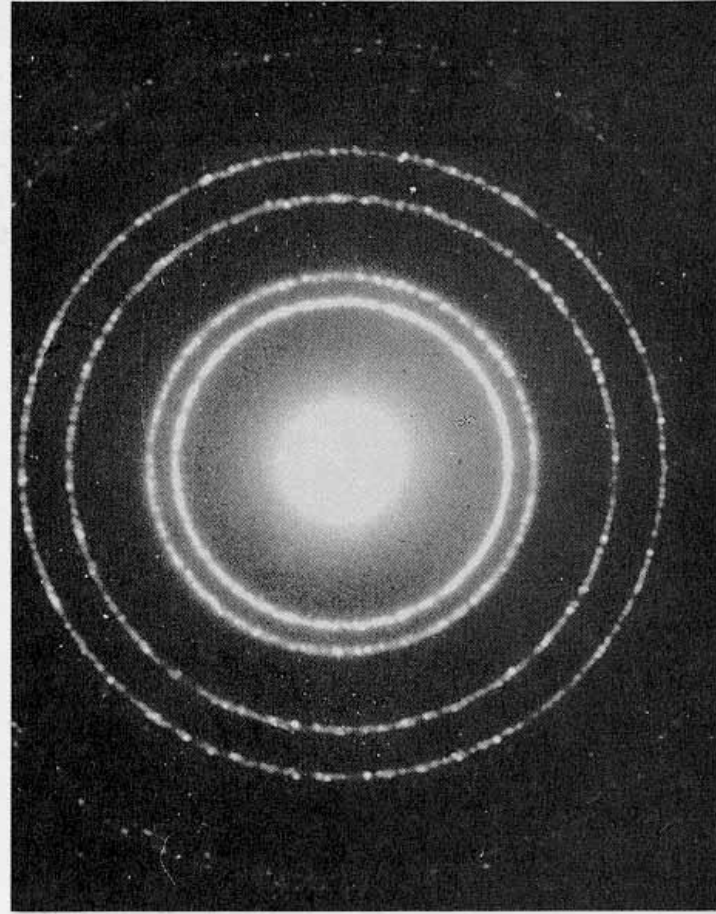
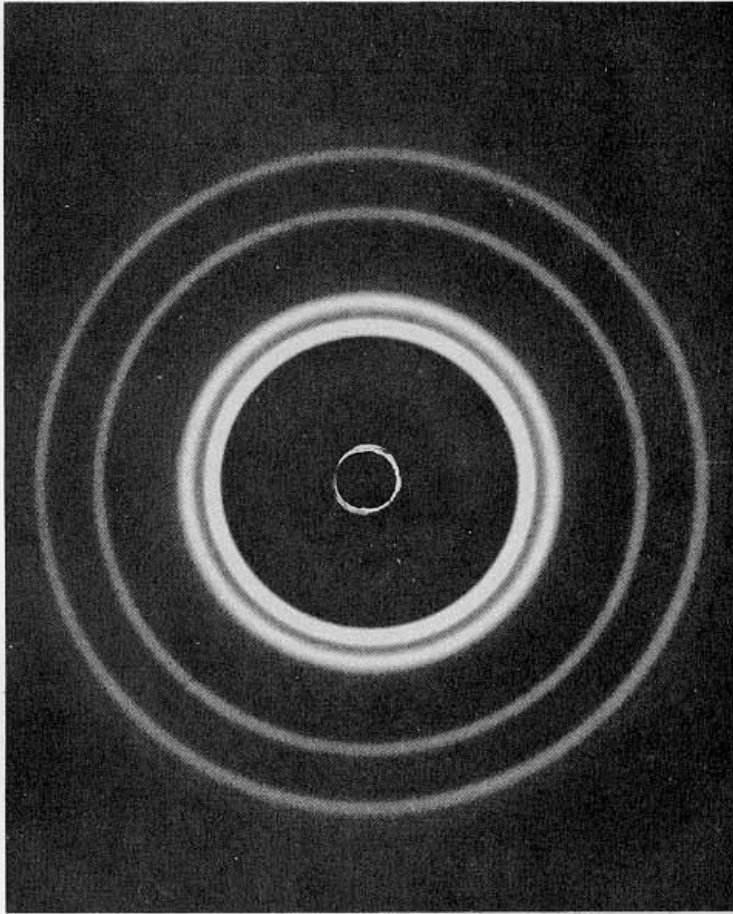
Bragg reflection

- Constructive interference when the path length difference is a integer multiple of the wavelengths
- $n\lambda = 2d \sin\theta$
- Detailed description requires heavy (mathematical) Quantum Mechanics.



The diffraction pattern on the left was made by a beam of x rays passing through thin aluminum foil. The diffraction pattern on the right was made by a beam of electrons passing through the same foil.

Diffraction Patterns



- Only certain angles of reflection are allowed.
- The diffracted electrons form patterns.
- In polycrystalline material, these are rings

X-rays on left,
electrons
on right.